

# **Styx: Unlinkable Anonymous Atomic Payment Hub For Viacoin**

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## **Abstract**

This paper presents Styx, an unlinkable anonymous atomic payment hub for Viacoin. In this paper we construct Styx which will provide strong anonymity. Our result is zero knowledge contingent payment proof. Styx is a payment scheme compatible with Viacoin protocol. This will allow participants to make payments faster and anonymously . Without any information leak that can lead to tell which payer paid during the epoch. A fair atomic exchange protocol which prevents theft of participants assets notably Viacoins.

The protocol combines off-the-blockchain cryptographic computations using Viacoin scripting functionalities and making use of security RSA assumptions, ROM and Elliptic Curve Digital Signature Algorithm.

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## 1.1 Fungibility

One of the most important properties of a currency is fungibility. For example, gold is fungible because 1g of gold is worth 1g of gold. So the real question here is what leads to this property because if that property were to be missing, fungibility would break down.

Gold is fungible because you cannot distinguish one bit of gold from another. There is no concept of old gold, new gold, or soiled gold so therefore all gold has the same value by weight. If there were, the gold from some sources may be less valuable. It would introduce the ability to blacklist.

There are many forms of digital payment systems where fungibility is a major concern. For example, Paypal have the ability to freeze accounts and payments at their sole discretion based on their opinion about the source or destination of payments being made on their platform.

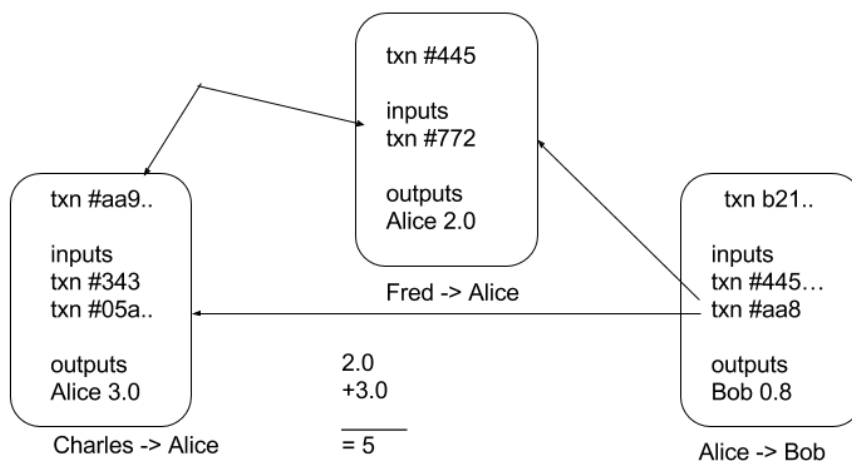
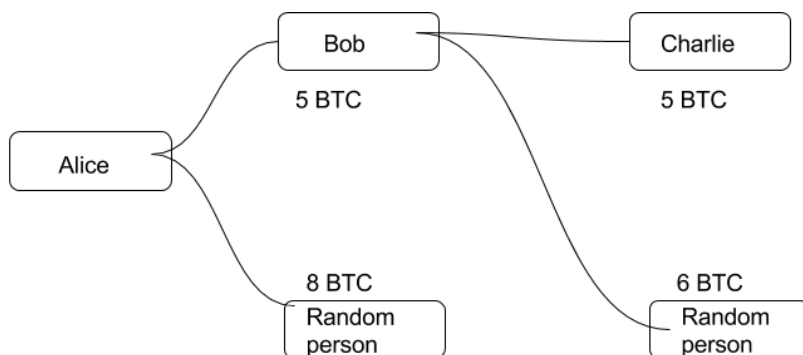
Centralized bitcoin payment providers like Coinbase often close down accounts because they believe payments are being received from, or being made to gambling sites. They can do this by looking at payment flows on the blockchain. Now if it were impossible to deduce where funds came from, or where they were being made to, it would be impossible to perform this kind of analytics and harm the fungibility of Bitcoin.

Because of the way payments are confirmed in Bitcoin like systems, it is, in theory possible for miners to blacklist specific coins from being spent at all. This was already tried in Ethereum after the infamous DAO hack. While some may view this as a legitimate case because it was viewed as theft, there is nothing stopping the same actions being taken against coins for other reasons.

So the solution is to make payments completely unlinkable to participants, or at least, provide a level of obfuscation to such a degree that looking at the blockchain transaction flow yield no meaningful information. This would make all payments equal as no payment could be tainted by the past, nor tainted by where the payment is going to.

Let's dive deeper into the specific problem.

Alice has sent Bob an amount of 5 coins. She must reference a payment where she received 5 or more coins. The nodes will check if Alice was the recipient and that the coins add up to 5 or more coins. Person Bob later on receives those same coins. When someone even looks at the transaction of Bob and Alice, they can even track back that a the person Charlie send coins to Alice.



Aside from the blockchain, nodes keep an extra database often called **UTXO**. UTXO stands for **Unspent Transaction Outputs**. The UTXO is a ledger that

records funds available for every address. It works like a cache for the blockchain. When new transactions are made, the UTXO will be updated. Addresses can be linked to one another by checking the transactions between them. Comparable to having a public ledger of bank statements .There are several ways to track down coins we present a few of them blow below :

### **-Transaction Graph and Off-network information:**

Is a graph where transactions are placed and connect a transaction input associated with the transaction output.

An attacker can link an address by searching info about the user online and in various public databases they might have access to. Many users have their coin address public on their internet forums profile or social media. Users who may expose their address on a website or forum. An attacker could then combine the information gained from the network analysis with other information or private database they have access to. This could be exchanges, online wallet services etc.

### **-IP traffic relays:**

An attacker can monitor the peer to peer payment network and observe which IP payments originate from.

### **-Cluster analysis:**

A clustering behavior in the user graph can help to reduce the size of the user graph. For example, payments sent to exchanges or gambling sites might be trivially identifiable.

Flow and temporal Analysis: Large flows of funds can be traced through the network of users. A user can be deduced out if at some point they receive an odd large flow compared to their account balance or tainted coins.

It should be very clear by now that transactions can be linked to specific users or services and this is how fungibility is harmed. The current design of Bitcoin and

cryptocurrencies based on Bitcoin do not have fungibility and every day as coin tracking becomes more advanced, fungibility is eroded.

To make **Viacoin** more robust and privacy-friendly it is essential to make sure Viacoin introduce fungibility to protect assets and increase user privacy and provide anonymous transactions between participants . It is our belief that only fungible digital currency will have a place in the future making this a top priority for Viacoin, which Viacoin users agreed with when surveyed .

A number of decentralized cryptocurrencies (e.g, Zerocash, Monero) have anonymous transactions implemented that are not compatible with Bitcoin. Viacoin is based on Bitcoin and it requires a robust, safe anonymity solution for the existing code base.

## 1.2 eCash Centralized anonymous payments

Before revealing the Viacoin anonymous payment system, recall ecash. The pre-Bitcoin payment scheme. It used to rely on a bank and it wasn't decentralized. It was a system to allow funds to be transferred anonymously, eCash used to charge sellers via paid fee.

eCash<sup>1</sup> used **blind signatures**<sup>2</sup> . With this system, no link can be made between withdraw & transaction. The eCash system ensured that payments could not be linked between payer A and receiver B. The unlinkability was achieved with use of blind signatures.

A blind signature can be instantiated with RSA. Signer has the RSA  $sk$  (secret key). He also has the  $pk$  (secret key) and  $pk$  (public key).  $pk$ ,  $N$  where  $N$  is the modulus.  $G$  as in full domain hash.  $A$  signs a message  $sn$ .  $A$  can produces blinded messages  $\bar{sn}$  by choose random blind  $r \leftarrow Z^*_N$

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<sup>1</sup> <https://www.win.tue.nl/~berry/papers/cosic.pdf>

<sup>2</sup> the message's content cannot be seen before it is signed

$$= r^{pk} G(m) \text{ mod } N_{RSA}^{-1}$$

Signer produces blind signature as:

$$\sigma = \frac{-1}{RSA} sk \text{ mod } N$$

A can unblind signature as:

$$\sigma = \sigma/r = (G(sn))^{sk} \text{ mod } N$$

This is how blind signatures are applied. This could be done with Viacoin if A sends S a viacoin and a blinded serial number  $\bar{sn}$  and A obtains a blind signature  $\sigma$ . A unblinds the values to create an anonymous voucher  $(sn, \sigma)$  which A can use to pay person B.

However this method is not robust. If S is malicious, he could steal by refusing to issue a blind signature to A in exchange for the received viacoins or refusing B anonymous voucher in exchange. This can be solved with using the Viacoin scripts that is able to enforce an atomic transaction mechanism. A swaps viacoin for a blind signature that's provided by S and in exchange swaps an anonymous voucher with B. An atomic exchange like this can be build with the Viacoin scripting functionalities.

## 2.1 Styx Fair Atomic Protocol

*Viacoin wallet is to atomic mix payments from payers.* Each atomic mix payment requires 3 confirmations. Nobody other than Payer A or B can determine linking. To make it DoS & Sybil<sup>3</sup> resistant we use fees. The use of *ephemeral keys*<sup>4</sup> to recover from malicious attackers that try to link A to B by payment abortion.

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<sup>3</sup> <http://freehaven.net/anonbib/cache/sybil.pdf>

<sup>4</sup> [https://en.wikipedia.org/wiki/Ephemeral\\_key](https://en.wikipedia.org/wiki/Ephemeral_key)

**S = Styx**

Allow A to swap Viacoin for an anonymous Voucher from S & allow B to provide T an anonymous Voucher in exchange for Viacoins. The Fair Atomic Protocol prevents S from stealing Viacoins by refusing to issue a voucher. The security rely on RSA and equivocal encryption in the ROM <sup>5</sup>(random oracle model).

Implement Atomic fair-exchange protocol using smart contracts with Viacoin current scripting functionality. It allows us to implement contracts that exchange a Viacoin for the preimage/hash or an Elliptic Curve Digital Signature Algorithm. Combined these limited scripting functionals (on the chain) with a crypto protocol performed off the chain to obtain the desired anonymity system we desire. The Crypto protocol will be fast. It can run in seconds because it rely on RSA blind signatures.

Every transaction decides the condition if a viacoin held in the transaction can be moved to another transaction. The rules are specified by Script. Script is stack-based and processed from left to right. Scripting provides the flexibility to change parameters or what's needed to spend the transferred Viacoins.

***Soffer** :transaction, one offers to pay Viacoin to any party that can sign a transaction who can meet some C as condition.*

***Sfulfill**:transaction, which meets C in Soffer*

Script will support time-locking for contracts (CHECKLOCKTIMEVERIFY). *Soffer* specify that a valid *Sfulfill* must be confirmed by the chain within a specific *tw* Time window. If this is not the case, the Viacoins in *Soffer* are no longer on offer to others.

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<sup>5</sup> <http://eprint.iacr.org/2015/140.pdf>



Hashing **OP\_RIPEDMD160** Condition  $C$  is specified in *Soffer*. *Sfulfill* must contain preimage of  $y$  under  $H$  hash function.  $H$  is **RIPEDMD160**. *Sfulfill* condition by  $x$  such that  $H(x) = y$

Signing condition **OP\_CHECKSIGVERIFY** The condition  $C$  is specified in *Soffer*. *Sfulfill* must be signed by a signature which verifies under  $PK$ , if this condition is valid signed by the secret key which correspond to  $PK$ . Viacoin requires the signature to be Elliptic Curve Digital Signature Algorithm over **Secp256k1** elliptic curve.

## **2.2 Styx RSA Atomic Fair exchange**

$A$  pays one Viacoin to  $S$  and  $S$  computing the RSA exponentiation to an RSA secret key  $sk$ . The protocol allows a user to bind a signature and bind a decryption.

$$\frac{-1}{RSA}(y, sk, N) = y^{sk} \bmod N$$

input chose by  $y$  by  $A$ ,  $sk$  is  $S$  secret RSA key and  $N$  RSA modulus. RSA verification is:

$$fRSA(x, pk, N) = x^{pk} \bmod N \text{ where } pk \text{ is } S \text{ public RSA key}$$

## **3.1 Zero knowledge contingent payments**

Swap Viacoins from  $A$  in exchange to have  $S$  compute any publicly verifiable function  $f$  on input of  $A$  choosing. After  $S$  computes the result of  $f(y)$  on input  $y$ . It will encrypt the results of under a randomly chosen key for obtaining  $c$  and hashes the encryption  $h = H(k)$ , then  $S$  sends  $A$  the  $c$  and  $h$  along with a zero knowledge proof. This without  $S$  revealing  $k$  of  $f(y)$  to person  $A$  before being paid with  $A$  Viacoins. After proof verified by  $A$ ,  $A$  posts a transaction *Soffer* to offer one Viacoin under condition **OP\_RIPEDMD160**.  $S$  will claim the Viacoin by posting transaction *Sfulfill* containing  $k$ .  $A$  will use  $k$  to decrypt  $c$  for  $f(y)$ . This is an atomic fair exchange because offered coins will be given back to  $A$  if  $S$  fails to post a valid *Sfulfill* within the time window.

### 3.2 Styx Zero knowledge Security Protocol Description

$\frac{-1}{RSA}$  is the trapdoor function,  $A$  could possibly learn preimages of random values without interaction  $F$ -atomic fair-RSA.  $A$  could “compute”  $mod N$  which  $A$  can know that  $y^{sk} mod N = x$ . To make this impossible, users will have to first blind their  $F$ -atomic~fair-RSA.

$S$  will be asked to provide  $n + m$  pairs.  $A$  will ask  $S$  to open  $n$  of these pairs, by revealing the randomly chosen keys  $k_i$ 's used to create each of the  $n$  pairs. In order for a malicious  $S$  to successfully attack  $A$  would have to correctly identify all the  $n$  challenge pairs and form them properly, while at the same time malforming all the  $m$  unopened pairs so it can claim a Viacoin from  $A$  without actually providing a **blind signature** in return.  $S$  cannot predict which pairs  $A$  asks it to open, it will succeed at its goal with an insanely very low probability. If  $A$  received the opening of  $(c, h)$  pair,  $A$  would be able to recover the blind signature without paying Viacoin. Serial numbers are random values  $sn$  have the value of a Viacoin. Fake values will be used, to specify  $n$   $(c, h)$ -pair that  $A$  asks  $S$  to decrypt to fake values instead of blind signatures. if  $S$  opens,  $A$  has to prove that  $n$  values are fake.

$$\delta_i = (\rho_i)^{pk} mod N$$

for random chose  $\rho_i \leftarrow R Z_N^*$ .  $A$  has to prove that the values of an input providing  $\rho_i$  to  $S$ . When  $S$  eval  $f(-1/RSA)$  on a fake input,  $\delta_i$

$$(\delta)^{sk} = ((\rho_i)^{pk})^{sk} = \rho_i mod N$$

$A$  knows.  $S$  will open  $(c, h)$  pairs responding to fake values while  $A$  has to be able to prove they are fake  $(c, h)$  values.  $A$  posts *Soffer* offering one viacoin for  $k$  which can open all of the  $m$  real  $(c, h)$  values. *Sfulfill* contains the hash preimages.

$A$  will obtain  $m$  blind signatures instead of 1. To make it fair, an extra step will be added.  $A$  posts *Soffer*,  $A$  proves  $S$  all  $m$  values have the same input and if  $S$  verifies,  $A$  posts *Sfulfill* to contain all  $m$  of  $k$  values that open real  $(c, h)$  pairs. Real  $m$  inputs that  $A$  sends to  $S$

$$d_j = y(r_j)^{pk} \bmod N$$

$d_j$  is  $y$  RSA blinded under different bind  $r_j \leftarrow \mathbb{R} \mathbb{Z}_n^*$  when  $S$  signs  $\frac{-1}{RSA}$  of real input  $d_j$   
 $(d_j)^{sk} = (y(r_j)^{pk})^{sk} = (y)^{sk} r_j \bmod N$

After A *Soffer* is confirmed by the chain, A prove  $S$  real inputs which correspond to  $d_j$ . A reveals all binds  $r_j$  to  $S$ .  $S$  redeem it Viacoin from A, *Sfulfill* containing  $k$  required to open  $(c,h)$  pairs. A can obtain the output of  $f^1$  on input  $y$  as long as 1 of  $(c,h)$  is validly formed and opened by a  $k$  value in *Sfulfill*.

#### 4.1 Styx Zero knowledge Security Voucher

Introducing voucher which can be used only with the viacoin-supported signature condition. *Sfulfill* must be signed by a signature which verifies under PK. The voucher is a transaction *Sfulfill* signed by Viacoin Elliptic Curve Digital Signature Algorithm over Secp256k1 elliptic curve (ECDSA-Secp256k1 signature). The signature will be computed under an *ephemeral* public key  $SK(eph/S)$ ,  $PK(eph/S)$  chosen by  $S$ .

$S$  post a **timelocked Soffer** offering 1 Viacoin in exchange for a valid voucher from  $B$ . It must be digitally signed by an **ECDSA-Secp256k1** that will verify under  $PK(eph/S)$  &  $PK_B$ .  $S$  redeems the voucher by  $B$  if submitted by  $B$ .

$B$  let  $S$  sign the voucher  $z = fRSA(\epsilon, pk, N)$

It's also possible for  $B$  to blind  $z$  before sending it to  $A$ . If  $A$  doesn't care about anonymity,  $B$  would still be anonymous.  $\epsilon$  let  $B$  open & encrypt  $c_e$  to a valid voucher. ECDSA-Secp256k1  $\sigma_e$  on a transaction *Sfulfill*.

$B$  creates a set  $\mu+n$  hash val  $B_e$  for  $l = 1 \dots \mu+n$ . By permutation of the hashes of the real and fake,  $B_e$  are send to  $S$ .  $S$  signs every  $B_e$  to obtain an ECDSA-Secp256k1  $\sigma_e$  and each is then hidden in inside  $C_e$  which is possible to decrypt with key  $\epsilon_e$ .  $S$  hides each encryption key  $\epsilon_e$  by using the RSA trapdoor function

$$z_e = f_{RSA}(\epsilon_e, pk, N)$$

$k$  pairs of will be send back to  $B$ .  $B$  must decide which encryption  $\epsilon_e$  to give to  $A$ . For Decryption  $B$  knows which  $C_e Z_e$  pair is valid formed. This can be done with chaining together  $\epsilon_e$  values that corresponds to real values.  $S$  provides  $B$  with  $\mu - 1$  quotients

$$q_2 = \epsilon_{j2}/\epsilon_{j1}, \dots, q_\mu = \epsilon_{j\mu}/\epsilon_{j\mu-1} \text{ mod } N$$

where  $j_1, \dots, j_\mu = R$  as in real values.  $\epsilon_{j1}$  allows  $B$  to recover of all other  $\epsilon_{j_e}$  since

$$\epsilon_{j_e} = \epsilon_{j1} * q_2 * \dots * q_e$$

$B$  asks  $A$  to invert  $z$ .  $A$  interacts with  $S$  to blindly invert  $Z$  by using the RSA  $sk$  in exchange for  $A$  Viacoin. Nobody can link  $S$  current interaction with  $A$  with value  $z$ .  $S$  won't be able to who is paying who.

Blind inversion,  $A$  will obtain preimage of  $z$  by contacting  $S$ .  $A$  binds to  $z$

$$y = z * r^{pk} \text{ mod } N$$

where  $r \leftarrow R \text{ mod } Z_N^*$  where  $R$  is the random chosen blind value.  $A$  will perform the RSA Atomic Fair exchange with  $S$  on input  $y$ .  $A$  swap Viacoin in exchange to  $y^{sk}$

$$y^{sk} = (z * r^{pk})^{sk} = (z)^{sk} * r = \epsilon * r \text{ mod } N$$

The result is the inversion of  $z$  blinded with  $r$ .  $A$  unblind

$$(y)^{sk} / r = \epsilon * r / r = \epsilon \text{ mod } N \text{ unveiling } \epsilon$$

$A$  sends  $\epsilon$  to  $B$  and uses  $\epsilon$  to open the  $c_e$  that contains the ECDSA-Secp256k1 signature  $\sigma_e$  on transaction  $S_{fulfill}$ . Finally  $B$  ECDSA signs  $S_{fulfill}$  under  $SK_B$  and post the result to the chain to claim his Viacoins from  $S$

## 4.2 Atomic anonymity

- Completeness       $B$  obtains  $z_i = f_{RSA}(\epsilon_i, pk, N)$  and  $c_i$  valid ECDSA-Secp256k1 signatures that can be unlocked with  $\epsilon_i$ .  $S$  issued locked signatures  $c_i$  that can be unlocked only if the A pays to learn  $f_{RSA}^{-1}(z_i, sk, N)$
- Fairness      If  $S$  is malicious there is a negligible probability that the atomic protocol successfully ends but  $B$  is not able to unlock  $c_i$ . If  $B$  is malicious, malicious  $S$  won't accept a voucher from  $B$ .  $S$  won't complete  $f_{RSA}$
- Anonymity       $A$ & $B$  should not be linkable.  $B$  provides  $z$  to  $A$  and  $A$  provides  $\epsilon$  to  $B$ . Communication between  $A$  and  $B$  is preserved.  $S$  or other 3rd party can use values to link payments.  $A$  "blinds"  $z$  to  $y$  before the atomic protocol with  $S$ .  $A$  will unblind results  $\epsilon$  and send it to  $B$
- Sybil & DoS       $S$  should not trust anyone. Use of anonymous vouchers is a blind signature which  $S$  can send to  $A$  in exchange for a payment.  $A$  is

able to buy vouchers in bulk before participation with  $S$ .  $A$  can unblind the vouchers and send it to  $B$  who will pass it to  $S$ . This is all done off-chain.

### 5.1 Overview

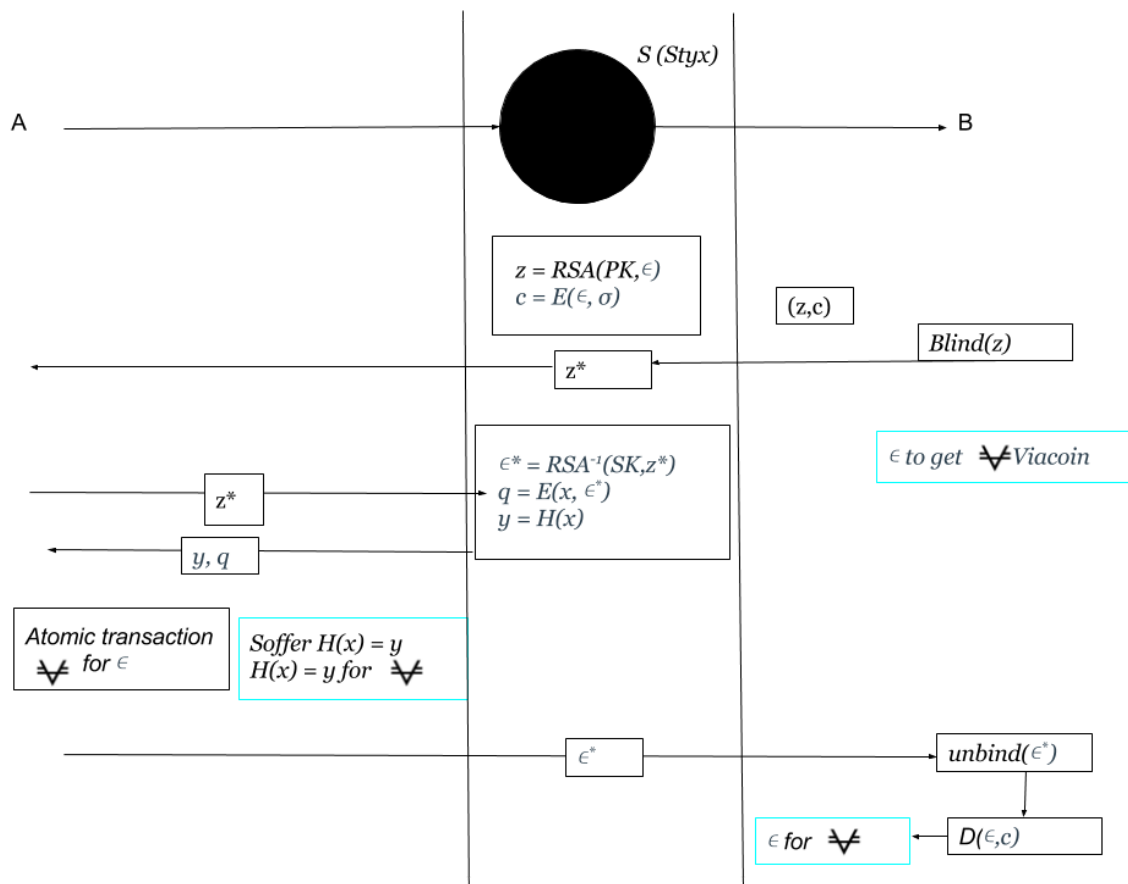


figure 1 Protocol overview

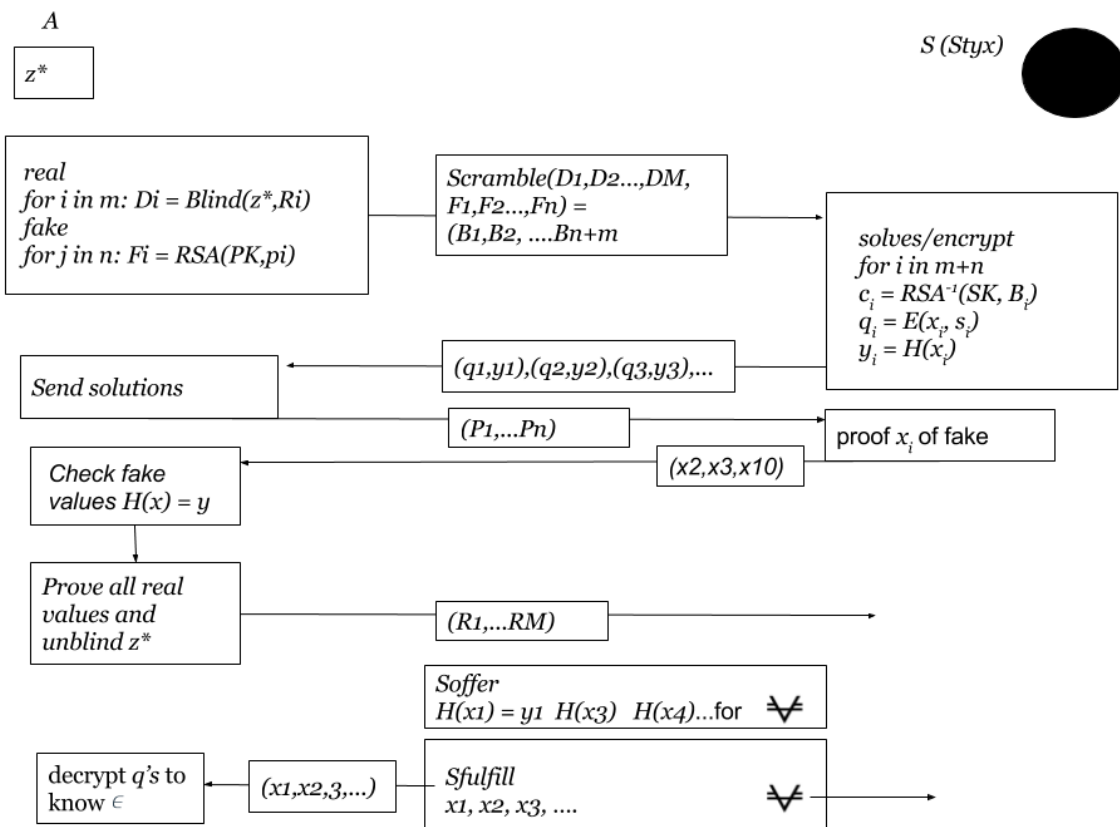


figure 2 Protocol solver

## 5.2 implementation

Instantiation of the protocol with 2048-bit RSA. Hash functions and signatures are instantiated as following.

Viacoin clients and miners operate transactions with the Viacoin script templates. Using P2SH transaction template that is used for standard transactions. This is a standard hash type.

*Soffer* P2SH transaction specified with the redeem script. Conditions must meet fulfill conditions of the transaction. The redeem script is hashed. The hash is stored in *Soffer*. For spending a transaction offer, the transaction fulfill has to be constructed.

*Sfulfill* includes the redeem script and a set of input values that the redeemsript is run against. The redeem script can be used for *fRSA*. The protocol can check that the input values in the transaction fulfill contain the preimages and the *Sfulfill* is signed by the public key of A. PubKey is *S* permanent viacoin address. Input values and redeem is run against the signature. It's a signature under the *S* permanent Viacoin address.

The real values RIPEMD-160 hash outputs must be stored in the redeem script (*fRSA*). P2SH redeem scripts are limited up to 520 bytes. increasing real values also increases transaction fees. Fees paid to (miners) confirm a transaction on the viacoin chain scale with the size of the transaction. The number of fake values can be bigger since they are handled completely off the chain. The real values can be under 20 and fake values under 300. We could minimize the RSA computations that he fake values are below 50.

### **Conclusion:**

Styx will be implemented as a layer on top of Viacoin and be compatible with the Viacoin protocol. Styx provides payments which are private. Privacy can't be violated and coins can't be stolen. Styx is a system that allows to make off-chain transactions with the same level of security as on-chain transactions. It's also an extra way to add anonymity and speedup transactions without choking the network.

Styx payment hub provides unlinkability during the payment phases. Because the use of off-chain transactions, the payments can be confirmed in seconds. Styx is possible because of existing opcodes that exist in viacoin, provides private and scalable payments while making it unlinkable to provide privacy and anonymity.



## 6.1 Acknowledgement

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